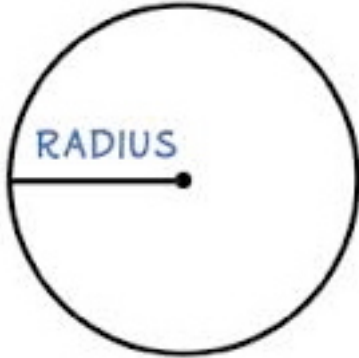


# DETERMINING VOLUME OF 3-D SHAPES

## Background Review:

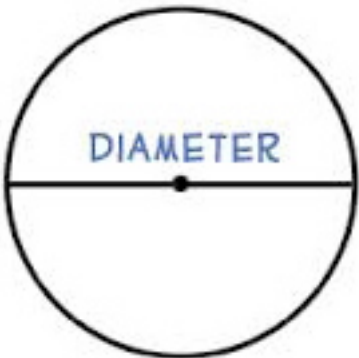
**RADIUS** (abbreviated “*r*”) – The distance from the center point of a circle to any point on the circle’s perimeter



The radius of a circle is half of the length of the diameter, so  $r = \frac{d}{2}$

Ex. If the diameter of a circle is 6 cm, the radius would be 3 cm.

**DIAMETER** (abbreviated “*d*”) – the length of a line segment that passes through the center of a circle dividing the circle into two equal halves.



The diameter of a circle is twice the length of the radius, so  $d = 2 \times r$

Ex. If the radius of a circle is 8 cm, the diameter would be 16 cm.

**CIRCUMFERENCE** (abbreviated “*c*”) – the entire distance around the outside of a circle



Pi, represented by the symbol “ $\pi$ ”, represents how many times longer a circle’s circumference is than its diameter (approximately 3.14 times).

Therefore, the length of a circle’s circumference is 3.14 times longer than its diameter, so  $c = \pi \times d$

### **Formulae:**

$$r = \frac{d}{2}$$

$$d = 2r$$

$$c = \pi d$$

$$r = \frac{c}{2\pi}$$

$$d = \frac{c}{\pi}$$

$$c = 2\pi r$$

## Background Review (continued):

**AREA** (abbreviated “*A*”) – the amount of space covered by a two dimensional shape

**SQUARE / RECTANGLE:** The area of a square or rectangle is calculated by multiplying its length by its width, so:

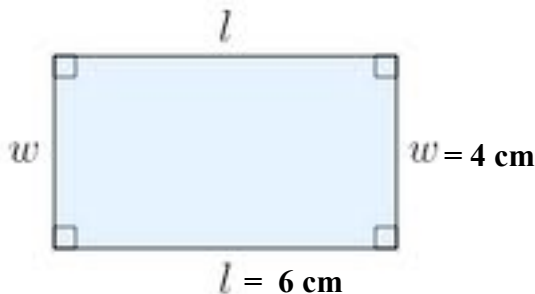
$$A = l \times w$$

*For the rectangle below:*

$$A = l \times w$$

$$A = 6 \text{ cm} \times 4 \text{ cm}$$

$$A = 24 \text{ cm}^2$$



**TRIANGLE:** The area of a triangle is always half of the area of a rectangle with the same sized base (or length in the rectangle) and the same sized height (or width in the rectangle). As a result, we can calculate the area of a triangle using the formula:

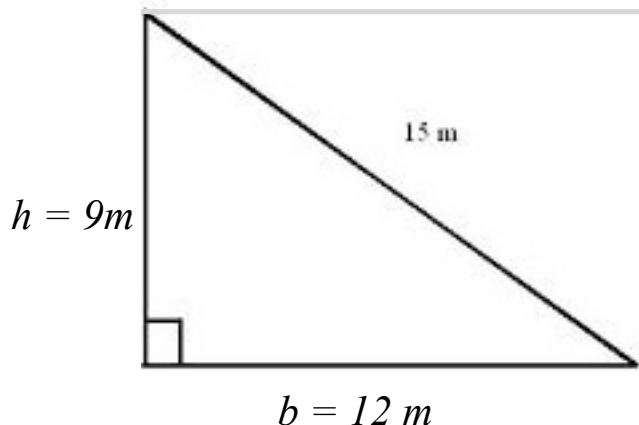
$$A = \frac{1}{2} \times b \times h$$

Look at the triangle below. Its base is 12 m and its vertical height is 9 m. To calculate its area, we simply use the formula  $A = \frac{1}{2} \times b \times h$  to calculate its area:

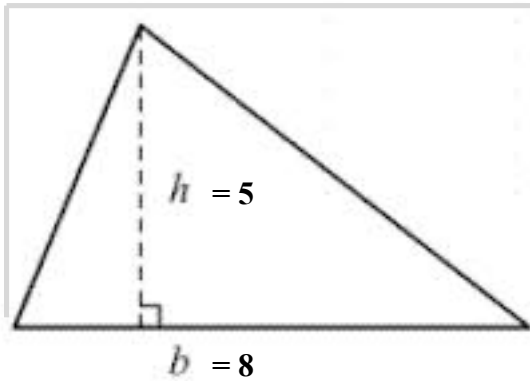
$$A = \frac{1}{2} \times b \times h$$

$$A = \frac{1}{2} \times 12\text{m} \times 9\text{m}$$

$$A = 54\text{m}^2$$



In the example below, the base is marked 'b' and the vertical height is marked 'h'. We use the same formula to calculate the area of this triangle ( $A = \frac{1}{2} \times b \times h$ )



$$\begin{aligned} A &= \frac{1}{2} \times b \times h \\ A &= \frac{1}{2} \times 8 \times 5 \\ A &= 20 \text{ square units} \end{aligned}$$

**NOTE:** In both triangles above, I have added light grey lines to show that triangles are indeed ALWAYS HALF OF A RECTANGLE.

**CIRCLE:** The area of a circle is calculated by multiplying *Pi* by the square of the length of the circle's radius, so:

$$A = \pi \times r^2$$

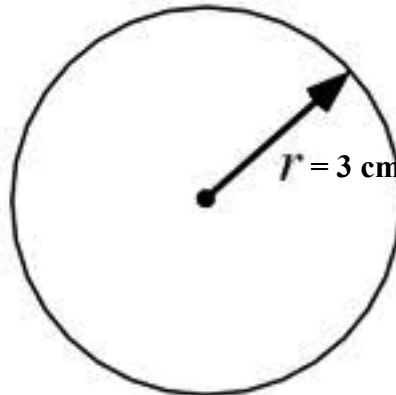
So for the circle below:

$$A = \pi \times r^2$$

$$A = 3.14 \times (3 \text{ cm})^2$$

$$A = 3.14 \times 9 \text{ cm}^2$$

$$A = 28.26 \text{ cm}^2$$



## Calculating Volume of a 3-D Object:

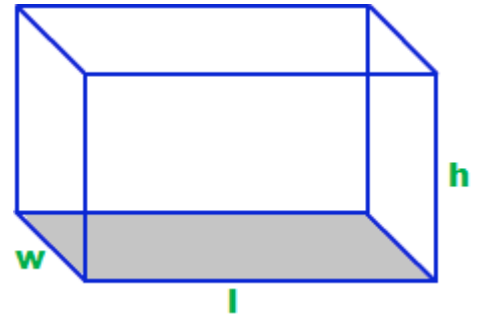
**VOLUME** (abbreviated “*V*”) – the amount of space the object occupies.

To calculate the volume of a rectangular prism or a cylinder, one must multiply the area of the object’s base by the height of the object.

**RECTANGULAR PRISM:** In a rectangular prism, the *base area* is calculated by multiplying length X width.

Therefore the formula for calculating the volume of a rectangular prism is:

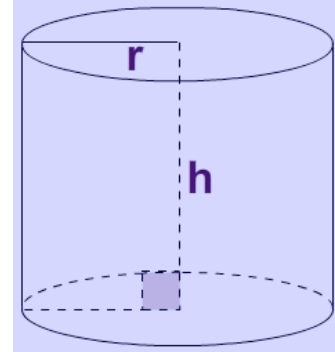
$$v = l \times w \times h$$



**CIRCLE:** In a cylinder, the base area is calculated by multiplying Pi by the square of the circle’s radius.

Therefore, the formula for calculating the volume of a cylinder is:

$$v = \pi \times r^2 \times h$$



**TRIANGULAR PRISM:** In a triangular prism, we must use a slightly different formula. Since a triangular prism has half the volume of a rectangular prism with the same height, we can calculate the volume of a triangular prism using the formula:

$$v = \frac{1}{2} \times b \times h \times l$$

